

Developing Generic Prior Distributions for Common Cause Failure Alpha Factors

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I. Introduction

- Common cause failures are significant risk contributors for commercial nuclear power plants
- Since 1980s, a series of reports have been published to provide guidelines for performing CCF modeling and performing CCF event data analysis
- A CCF database system has been developed and maintained by INL for the NRC for U.S. commercial nuclear power plants
 - CCF database: stores coded CCF events
 - CCF software: uses impact vectors and mapping methods to estimate CCF parameters
- Generic prior distributions were developed and included in the CCF software for CCF Alpha Factor Model (AFM) parameter estimations

I. Introduction (cont.)

- The CCF database system has been maintained since its development in late 1990s
- The CCF parameter estimations have been updated and published on a yearly basis
- However, the process for developing prior distributions has not been published
- The prior distributions have not been updated since early 2000s
- Let's
 - Review the CCF analysis history
 - Review the prior distribution development process
 - Update the prior distributions
 - Discuss issues in the process

II. History of CCF Analysis

- NUREG/CR-4780, *Procedures for Treating Common Cause Failures in Safety and Reliability Studies*, January 1988
 - Presents the framework for including CCFs in risk and reliability evaluations with four major stages
 - Introduces the concept of impact vectors and the mapping method
- NUREG/CR-6268, *Common Cause Failure Database and Analysis System*, June 1998
 - Method to collect data, characterize CCF events, and estimate CCF parameters and uncertainties
 - A CCF database system and the CCF software
- NUREG/CR-5497, *Common-Cause Failure Parameter Estimations*, October 1998
 - Quantitative results and insights
- NUREG/CR-5485, *Guidelines on Modeling Common-Cause Failures in Probabilistic Risk Assessment*, November 1998
 - Guidelines to model CCF events in PRA

II. History of CCF Analysis (cont.)

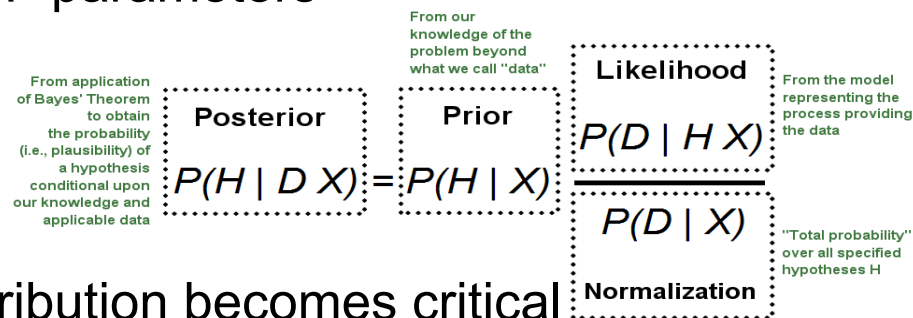
- NUREG/CR-6268, Revision 1, *Common Cause Failure Database and Analysis System, Event Data Collection, Classification, and Coding*, September 2007
 - Update the guidance for collecting, classifying, and coding CCF events described in its older version published in 1998
- A series of NRC/INL reports were published on the NRC web site, <http://nrcoe.inl.gov/resultsdb>, to update the CCF parameter estimations
 - *2003 Update*, data from 1985 to 2003
 - *2005 Update*, data from 1991 to 2005
 - *2007 Update*, data from 1991 to 2007
 - *2009 Update*, data from 1997 to 2009
 - *2010 Update*, data from 1997 to 2010
 - *2012 Update*, data from 1997 to 2012
 - *2015 Update*, data from 1997 to 2015

II. History of CCF Analysis (cont.)

- Quality control in the process of data classification, loading, and parameter estimation
 - All events are reviewed by two INL data analysts to make sure that the events are classified as CCF events and coded correctly
 - A PRA analyst reviews the CCF events and results for consistency and comparison with PRA experience
 - A final review is performed by independent CCF expert(s) outside of INL
- Still, the CCF event identification and characterization are subject to engineering judgement
 - Different analysts have different interpretations of the events
 - Different degrees of available information
- Uncertainty caused by data and methodology should be identified

III. Existing CCF Priors

- Bayesian estimation procedure is used to develop uncertainty distributions for CCF parameters



- Choice of prior distribution becomes critical
 - Analyst's subjective judgement or
 - Based on observed CCF data and applicable methodology
- NUREG/CR-5485 uses a mapping method to develop prior distributions for alpha factors
 - Utilize all CCF events in database by mapping to a given CCGG size.
 - MLE for each alpha factor is obtained and fit with constrained noninformative distribution
 - The estimates of the Dirichlet distribution parameters are calculated and combined to obtain an effective estimate
- No details on developing prior distributions

III. Existing CCF Priors (cont.)

Mean Values of Existing CCF Prior Parameters

Parameter	NUREG/ CR-5485	2003 CCF Update	2005 CCF Update	2007 CCF Update	2010 White Paper	2009, 2010, 2012, and 2015 CCF Update
Range of Data	1980–1995	1985–2003	1991–2005	1991–2007	1995–2005	1997–2009 (2010,2012,2015)
α_2 (CCCG=2)	4.70E-02	3.09E-02	4.06E-02	2.57E-02	1.75E-02	Same as in the 2007 CCF Update Report
α_3 (CCCG=3)	2.58E-02	7.17E-03	8.71E-03	5.79E-03	5.94E-03	
α_4 (CCCG=4)	1.86E-02	3.72E-03	4.64E-03	2.98E-03	3.81E-03	
α_5 (CCCG=5)	1.46E-02	6.26E-04	7.25E-04	5.33E-04	9.32E-04	
α_6 (CCCG=6)	1.23E-02	6.15E-04	6.86E-04	4.07E-04	5.06E-04	
α_7 (CCCG=7)	1.03E-02	1.29E-04	1.52E-04	1.17E-04	2.22E-04	
α_8 (CCCG=8)	9.06E-03	1.38E-04	1.46E-04	1.25E-04	1.88E-04	

IV. Updating Priors for Alpha Factors

- Step 1. For each CCCG size, tabulate the number of CCF events and complete CCF events
- Step 2. For partial CCF events, calculate n_k for each group size with mapping methodology
- Step 3. For complete CCF events, perform a binomial regression to obtain the probability of complete CCF events and then estimate the number of complete CCF events for each group size
- Step 4. Add results from Step 3 to the final n_k for each group size (add the number to n_2 for group size 2, n_3 for group size 3, etc.)
- Step 5. Using the final n_k values, estimate the mean values of alpha factors for each group size
- Step 6. Using computer code, CalcPrior, developed by INL to estimate the distributions of the alpha factors with a procedure to calculate Dirichlet distribution parameters with noninformative prior distributions

IV. Updating Priors for Alpha Factors (cont.)

- Access CCF data
 - NRC CCF Database website <https://rads.inl.gov/Pages/CCF.aspx>
 - Query the CCF Database directly with SQL Server
- This prior update uses data from 1997 through 2015
- A total of 268 CCF events (56 complete, 212 partial CCF) and 7492.8 effective independent failure events

IV. Updating Priors for Alpha Factors (cont.)

CCF Data 1997-2015

Group Size	No. Partial CCF Events	No. Complete CCF Events	Total No. CCF Events	Prob. of Complete CCF Event - Data	Prob. of Complete CCF Event - Curve Fitting	Estimated No. Complete CCF Events	n_k Values for Partial CCF Events										
2	27	34	61	0.55738	0.51050	31.14031											
3	27	12	39	0.30769			Group Size	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8		
4	61	2	63	0.03175			2	115.61	31.164								
5	7	0	7	0.00000			3	109.23	64.693	9.267							
6	30	5	35	0.14286			4	96.47	80.938	25.857	4.038						
7	3	0	3	0.00000			5	96.92	73.190	39.900	14.539	2.141					
8	30	2	32	0.06250			6	98.05	65.654	46.584	23.001	8.533	1.209				
9	0	0	0				7	101.15	61.106	44.388	29.499	15.401	5.219	0.716			
10	0	0	0				8	102.97	59.825	41.221	31.486	20.828	10.368	3.197	0.453		
11	5	0	5	0.00000													
12	7	1	8	0.12500	0.07153	0.57226											
13	0	0	0		0.07151	0.00000											
14	1	0	1	0.00000	0.07150	0.07150											
15	0						Group Size	n_t	n_l	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8
16	14						2	3042.49	2864.58	115.61	62.304						
Total	212						3	4491.83	4296.87	109.23	64.693	21.038					
							4	5947.30	5729.16	96.47	80.938	25.857	14.873				
							5	7388.92	7161.45	96.92	73.190	39.900	14.539	2.919			
							6	8839.80	8593.74	98.05	65.654	46.584	23.001	8.533	4.237		
							7	10283.74	10026.03	101.15	61.106	44.388	29.499	15.401	5.219	0.948	
							8	11731.02	11458.32	102.97	59.825	41.221	31.486	20.828	10.368	3.197	2.807

Adjusted n_k

IV. Updating Priors for Alpha Factors (cont.)

Updated Alpha Factor Mean Values (1997-2015)

Group Size	α_1	α_2	α_3	α_4	α_5	α_6	α_7	α_8
2	0.9795	2.048E-02						
3	0.9809	1.440E-02	4.684E-03					
4	0.9795	1.361E-02	4.348E-03	2.501E-03				
5	0.9823	9.905E-03	5.400E-03	1.968E-03	3.951E-04			
6	0.9833	7.427E-03	5.270E-03	2.602E-03	9.653E-04	4.793E-04		
7	0.9848	5.942E-03	4.316E-03	2.869E-03	1.498E-03	5.075E-04	9.214E-05	
8	0.9855	5.100E-03	3.514E-03	2.684E-03	1.775E-03	8.838E-04	2.725E-04	2.393E-04

IV. Updating Priors for Alpha Factors (cont.)

Updated Alpha Factor Prior Distributions (1997-2015)

Group Size	a1	b1	a2	b2	a3	b3	a4	b4
2	2.2413E+01	4.6853E-01	4.6853E-01	2.2413E+01				
3	5.7979E+01	1.1280E+00	8.5122E-01	5.8255E+01	2.7682E-01	5.8830E+01		
4	9.0676E+01	1.8936E+00	1.2597E+00	9.1310E+01	4.0244E-01	9.2167E+01	2.3148E-01	9.2338E+01
5	1.9084E+02	3.4322E+00	1.9242E+00	1.9235E+02	1.0490E+00	1.9322E+02	3.8224E-01	1.9389E+02
6	2.2522E+02	3.8349E+00	1.7011E+00	2.2735E+02	1.2070E+00	2.2785E+02	5.9596E-01	2.2846E+02
7	3.7180E+02	5.7474E+00	2.2432E+00	3.7530E+02	1.6295E+00	3.7591E+02	1.0829E+00	3.7646E+02
8	3.9002E+02	5.7256E+00	2.0181E+00	3.9373E+02	1.3905E+00	3.9436E+02	1.0621E+00	3.9469E+02
Group Size	a5	b5	a6	b6	a7	b7	a8	b8
2								
3								
4								
5	7.6743E-02	1.9420E+02						
6	2.2109E-01	2.2883E+02	1.0978E-01	2.2895E+02				
7	5.6537E-01	3.7698E+02	1.9159E-01	3.7735E+02	3.4801E-02	3.7751E+02		
8	7.0259E-01	3.9505E+02	3.4974E-01	3.9540E+02	1.0784E-01	3.9564E+02	9.4689E-02	3.9565E+02

V. Issues and Discussions

- Is the mapping method appropriate for CCF parameter estimations or prior determination? Are there any other alternative approaches to develop the prior distributions?
- Is the using of binomial regression treatment of complete CCF events in the current process appropriate? What should be the proper model to be used for curve fitting?
- Should different prior distributions be developed for different component groups?
- Will the testing scheme for various components impact priors?

Questions?

